# CS 295: Optimal Control and Reinforcement Learning

#### Winter 2020

# Assignment 3

#### due Tuesday, February 18 2020, 11pm

#### Part I

Consider the empirical estimation of the advantage of action a in state s, upon seeing (s, a, r, s'), as  $\hat{A}(s, a) = r + \gamma V(s') - V(s)$ . For the purpose of this question, we'll make the following assumptions:

- $V = V_{\pi}$  is the true state-value function of the policy of interest  $\pi$ ;
- The experience (s, a, r, s') is sampled by rolling out  $\pi$ ;
- r(s, a) is a deterministic function of the state s and action a; and
- $V(s) \in [-1, 1]$  for all s.
- 1. Remind yourself that  $\mathbb{E}_{a|s\sim\pi}[\hat{A}(s,a)]=0$ , by definition of  $V_{\pi}$ . What conditional distribution of  $V(s')\in[-1,1]$ , given s and a, induces the worst-case conditional variance of  $\hat{A}(s,a)$ ?
- 2. What is  $\mathbb{E}[V(s')|s,a]$ ? What can you conclude about r(s,a)?
- 3. Suggest a two-state process (MDP and policy) that has the worst-case conditional variance of  $\hat{A}(s,a)$  in each state and action. Specify p(s'|s,a), r(s,a), and  $\pi(a|s)$  for each s, a, and s'. Don't worry if the process is very degenerate, in fact try to make it as simple as possible. Hint: originally, the policy was omitted in this question, because in the simplest worst-case MDP the policy doesn't make a difference.
- 4. In the process you proposed above, what is the conditional variance, given  $s_t$  and  $a_t$ , of each of the following advantage estimators on on-policy experience  $(s_t, a_t, r_t, s_{t+1}, \ldots)$ ?
  - (a)  $\hat{A}^{MC}(s_t, a_t) = \sum_{t' \ge t} \gamma^{t'-t} r_{t'} V(s_t).$
  - (b)  $\hat{A}^n(s_t, a_t) = \sum_{t'=t}^{t+n-1} \gamma^{t'-t} r_{t'} + \gamma^n V(s_{t+n}) V(s_t)$ ; which n minimizes the conditional variance under the question's assumptions?
  - (c) **Bonus:**  $\hat{A}^{\lambda}(s_t, a_t) = (1 \lambda) \sum_{n \geq 1} \lambda^{n-1} \hat{A}^n(s_t, a_t) = \sum_{t' \geq t} \gamma^{t'-t} \hat{A}^1(s_{t'}, a_{t'})$ ; Hint: careful, these  $\hat{A}$  aren't conditionally independent.

#### Part II

## 1 Advantage Actor-Critic

In this part you'll implement several actor—critic algorithms, starting with Advantage Actor—Critic (A2C; https://arxiv.org/abs/1602.01783). Note: in RLlib it's easy to distribute the algorithm's execution using Ray, by setting the num\_workers in the Tune configuration. If the distribution is asynchronous (which is not the default), this would then be the A3C algorithm.

Download the code at https://royf.org/crs/W20/CS295/A3/a2c.py. In the function actor\_critic\_loss, write TensorFlow code that calculates a loss with 3 terms:

- A policy-gradient loss with advantage estimation;
- A temporal-difference loss for the value function, weighted by v\_loss\_coeff; and
- Bonus: a negative-entropy loss on the policy, weighted by ent\_loss\_coeff (i.e. a slight push to *maximize* entropy). First try without it, and then add it and compare. Hint: action\_dist.entropy() can come in handy.

In the function postprocess\_advantages, recall that sample\_batch is part of a single trajectory, but in this assignment we will **not** assume that it's the entire trajectory. Write code that calculates the scalar last\_value\_pred, i.e. the critic's prediction of the expected return following the last s' (a.k.a next\_obs) in the sample. Useful: (1) policy.\_value, a function that gets an array of observations (a.k.a states, when observability is full) and returns a same-size array of value predictions (you can see below how it's implemented); and (2) dones, a boolean array indicating termination in each time step (hint: why is this useful here?).

Also write NumPy code that calculates the discounted one-step advantages and value targets.

Run your code on the CartPole-v1 environment for 1000000 time steps.

### 2 Generalized Advantage Estimation

Create a copy of a2c.py called gae.py, and change it to implement the GAE algorithm (see https://arxiv.org/abs/1506.02438, also question 4c in Part I). Recall the helper function ray.rllib.evaluation.postprocessing.discount.

Run your code on CartPole-v1 with a variety of  $\lambda$  values. Tip: by setting the name of the trainer to include the value of  $\lambda$ , you can easily see it later in TensorBoard.

Visualize the results in TensorBoard, and attach the resulting plots. Briefly discuss the results, including:

- What was the best value of  $\lambda$  in your experiments?
- What happens as  $\lambda \to 0$ ?
- What happens as  $\lambda \to 1$  in theory? What happens in practice?